Geometry September 23, 2013
Reflections and Rotations with Change of Coordinates

Name period

1. Complete the table: Record the coordinates of the images resulting from a reflection of the pre-image points in the line $y=0$ which is the equation of the -axis.
(Can you do this without graphing?)

| Pre-image | Image |
| :--- | :--- |
| a. $(4,7)$ |  |
| b. $(-2,-9)$ |  |
| c. $(3,-8)$ |  |
| d. $(-6,1)$ |  |
| e. $(x, y)$ |  |

2. Complete the table: Record the coordinates of the images resulting from a reflection of the pre-image points in the line $x=0$ which is the equations of the __-axis.
(Can you do this without graphing?)

| Pre-image | Image |
| :--- | :--- |
| a. $(-3,9)$ |  |
| b. $(5,-2)$ |  |
| c. $(7,8)$ |  |
| d. $(-6,-1)$ |  |
| e. $(x, y)$ |  |


3.

Reflect $\triangle P Q R$ in the line $y=x$. Label $\Delta P^{\prime} Q^{\prime} R^{\prime}$ and record the image coordinates in the table below. Generalize for any $(x, y)$.

| Pre-image | Image |
| :--- | :--- |
| $P(-5,5)$ |  |
| $Q(-2,4)$ |  |
| $R(-3,2)$ |  |
| $(x, y)$ |  |


4.

Reflect $\Delta K L M$ in the line $y=-x$. Label $\Delta K^{\prime} L^{\prime} M^{\prime}$ and record the image coordinates in the table below. Generalize for any $(x, y)$.

| Pre-image | Image |
| :--- | :--- |
| $K(-4,-2)$ |  |
| $L(-2,-3)$ |  |
| $M(-5,-5)$ |  |
| $(x, y)$ |  |


5.

Reflect $\triangle X Y Z$ in the line
$y=\frac{-1}{2}(x+5)+4$. Graph the line.
Label $\Delta X^{\prime} Y^{\prime} Z^{\prime}$ and record the image coordinates in the table below.

| Pre-image | Image |
| :--- | :--- |
| $X(5,5)$ |  |
| $Y(4,2)$ |  |
| $Z(2,3)$ |  |
| Currently, we do not know how to |  |
| generalize this reflection. |  | $\quad$

6. Rotate the shape lying on the
x-axis $90^{\circ}, 180^{\circ} \& 270$
clockwise about the origin.


Record the coordinates of the images of point A rotated $90^{\circ}, 180^{\circ} \& 270^{\circ}$ clockwise about the origin.

| Pre-image | $A(-4,-2)$ |
| :--- | :--- |
| Rotation | clockwise |
| $90^{\circ} \mathrm{CW}$ |  |
| $180^{\circ} \mathrm{CW}$ |  |
| $270^{\circ} \mathrm{CW}$ |  |

7. Rotate the shape lying on the x-axis $90^{\circ}, 180^{\circ} \& 270$ clockwise about the origin.


Record the coordinates of the images of point B rotated $90^{\circ}, 180^{\circ} \& 270^{\circ}$ clockwise about the origin.

| Pre-image | $B(2,3)$ |
| :--- | :--- |
| Rotation | clockwise |
| $90^{\circ} \mathrm{CW}$ |  |
| $180^{\circ} \mathrm{CW}$ |  |
| $270^{\circ} \mathrm{CW}$ |  |

8. Rotate the shape lying on the x-axis $90^{\circ}, 180^{\circ} \& 270^{\circ}$ clockwise about the origin.

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Record the coordinates of the images of point C rotated
$90^{\circ}, 180^{\circ} \& 270^{\circ}$ clockwise about the origin.

| Pre-image | $C(1,-5)$ |
| :--- | :--- |
| Rotation | clockwise |
| $90^{\circ} \mathrm{CW}$ |  |
| $180^{\circ} \mathrm{CW}$ |  |
| $270^{\circ} \mathrm{CW}$ |  |

9. Examine the relationship between the pre-image and image points in \# 6-7-8 above to find the general pattern. When any $(x, y)$ point is rotated about the origin $90^{\circ} C W$ the resulting image has coordinates $\qquad$ .

When any $(x, y)$ point is rotated about the origin $180^{\circ} C W$ the resulting image has coordinates $\qquad$ .

When any $(x, y)$ point is rotated about the origin $270^{\circ} \mathrm{CW}$ the resulting image has coordinates $\qquad$ .
10. Reflect hexagon KLMNOP in the line $y=x$.

11. Rotate hexagon KLMNOP $90^{\circ}, 180^{\circ} \& 270^{\circ}$
clockwise about the origin.


