Geometry
Module 7.6

Name period 1 2

Shifty Functions: We will use the TI-84 graphing calculator to examine transformations of functions.
Write the equation for the graph of $f(x)$ shown on the coordinate grid. Graph $f(x)$ on the TI-84. Also graph $g(x)$ and $h(x)$ using function notation on the TI-84. Describe in words $g(x)$ and $h(x)$ as transformations of $f(x)$.

1. $f(x)=$ $\qquad$
$g(x)=f(x)+2$
describe:
$h(x)=f(x+4)$ describe:

2. $f(x)=$ $\qquad$
$g(x)=f(x)-3$
describe:
$h(x)=f(x-3)$
describe:

3. $f(x)=$ $\qquad$

$$
g(x)=f(x)-1
$$

describe:

$$
h(x)=f(x-4)
$$

describe:


Shifty Shapes: Use the vertical and horizontal shifting ideas from above to graph and describe the transformations of the shape below.

Let's call the shape below... $\operatorname{Shape}(X)$ which we say and read as "Shape of $X$ "
4. Graph: Shape(X)-5

Describe:

Graph: $\quad$ Shape $(X+5)$
Describe:

5. Graph:

Shape(X) +6
Describe:

Graph:
Describe:

|  |  |  |  | $\mathbf{Y}$ |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

6. Graph: $\quad \operatorname{Shape}(X)-4$ Describe:

Graph: $\quad \operatorname{Shape}(X+4)$
Describe:

|  |  |  |  | $\mathbf{Y}$ |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
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|  |  |  |  |  |  |  |  |  | $\mathbf{X}$ |
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## Shifting Functions using Tables:

- Re-write $g(x)$ and $h(x)$ in terms of $x$, rather than $f(x)$ as given.
- Complete the table of values $f(x), g(x)$ and $h(x)$ for the given $x$-values.
- Graph all three functions on the same coordinate grid.
- Describe how $\mathrm{g}(\mathrm{x})$ values and $\mathrm{h}(\mathrm{x})$ values are transformed from $\mathrm{f}(\mathrm{x})$ values.

7. 

$f(x)=\frac{1}{2} x, \quad g(x)=f(x)+3, \quad h(x)=f(x-3)$

$$
g(x)=\quad h(x)=
$$

$\qquad$

| $x$ | -3 | -2 | -1 | 0 | 1 | 2 | 3 | 4 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $f(x)$ |  |  |  |  |  |  |  |  |
| $g(x)$ |  |  |  |  |  |  |  |  |
| $h(x)$ |  |  |  |  |  |  |  |  |

Describe $g(x)$ as a translation of $f(x)$ :


Describe $h(x)$ as a translation of $f(x)$ :
8. Remember order of operations when completing the table.
$f(x)=x^{2}, \quad g(x)=f(x)-3, \quad h(x)=f(x+3)$
$g(x)=\ldots \quad h(x)=\ldots$

| $x$ | -3 | -2 | -1 | 0 | 1 | 2 | 3 | 4 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $f(x)$ |  |  |  |  |  |  |  |  |
| $g(x)$ |  |  |  |  |  |  |  |  |
| $h(x)$ |  |  |  |  |  |  |  |  |



Describe $\mathrm{g}(\mathrm{x})$ as a translation of $\mathrm{f}(\mathrm{x})$ :
9. Matching: Fill in the Description Letter and the Transformation Letter in the column to match the $p(x)$ image function equation in the left-hand column.

The Pre-Image Functions are listed here:

$$
f(x)=x \quad g(x)=-x \quad h(x)=\frac{1}{2} x \quad j(x)=-2 x \quad k(x)=3 x \quad m(x)=-\frac{1}{3} x
$$

| Image Functions | Descr LETTER | Trans LETTER |  | Description | Transformation Equation |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $1 p(x)=x+5$ |  |  | A | Translate $\mathrm{g}(\mathrm{x})$ left 7 units | $p(x)=k(x-5)$ |
| $2 p(x)=\frac{1}{2} x-7$ |  |  | B | Translate j(x) left 3 units \& down 4 units | $p(x)=m(x-4)+3$ |
| $3 \quad p(x)=3(x-5)$ |  |  | C | Translate $\mathrm{k}(\mathrm{x})$ right 5 units | M $p(x)=j(x+3)-4$ |
| $4 \quad p(x)=-(x+7)$ |  |  | D | Translate $\mathrm{h}(\mathrm{x})$ right 5 units \& down 7 units | $p(x)=h(x)-7$ |
| $5 \quad p(x)=-2(x+3)-4$ |  |  | E | Translate $m(x)$ right 4 units \& up 3 units | $p(x)=h(x-5)-7$ |
| $p(x)=-\frac{1}{3}(x-4)+3$ |  |  | F | Translate $\mathrm{h}(\mathrm{x})$ down 7 units | $p(x)=f(x)+5$ |
| $7 \quad p(x)=\frac{1}{2}(x-5)-7$ |  |  |  | Translate $\mathrm{f}(\mathrm{x})$ up 5 units | R $p(x)=g(x+7)$ |

10. Communicate Your Understanding:

If $f(x)=g(x)+k$, describe the transformation to $\mathrm{g}(\mathrm{x})$ that produces $\mathrm{f}(\mathrm{x})$ when ...the k-value is positive:
...the k-value is negative:

If $f(x)=g(x-h)$, describe the transformation to $g(x)$ that produces $f(x)$ when ...the h-value is positive:
...the $h$-value is negative:

If $f(x)=g(x-h)+k$, describe the transformation to $g(x)$ that produces $f(x)$ when ...the $h$-value and k-value are positive: ...the h-value and k-value are negative:

Topic: Vertical translations of linear equations
The graph of $f(x)$ and the translation form equation of $g(x)$ are given. Graph $g(x)$ on the same grid and write the slope-intercept equation of $f(x)$ and $g(x)$.
11. $g(x)=f(x)-5$
a.

b. $f(x)=$ $\qquad$
c. $g(x)=$ $\qquad$
$12 g(x)=f(x)+4$
a.

b. $f(x)=$ $\qquad$
c. $g(x)=$ $\qquad$
13. $g(x)=f(x)-6$
a.

b. $f(x)=$ $\qquad$
c. $g(x)=$ $\qquad$

## Topic: Horizontal translations of linear equations

The graph of $f(x)$ and the translation form equation of $g(x)$ are given. Graph $g(x)$ on the same grid and write the slope-intercept equation of $f(x)$ and $g(x)$.
14. $g(x)=f(x+6)$
a.

b. $f(x)=$ $\qquad$
c. $g(x)=$ $\qquad$
15. $g(x)=f(x+5)$
a.

b. $f(x)=$ $\qquad$
c. $g(x)=$ $\qquad$
Slope-Intercept form
16. $g(x)=f(x-4)$
a.

b. $f(x)=$ $\qquad$
c. $g(x)=$ $\qquad$

